## 6.S077: Introduction to Low-level Programming in C and Assembly Spring 2023, Quarter 1

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| :--- | :--- |
|  | MIT ID \#: |


| $\# 1(15)$ | 15 |
| :--- | ---: |
| $\# 2(6)$ | 6 |
| $\# 3(10)$ | 10 |
| $\# 4(24)$ | 24 |
| $\# 5(10)$ | 10 |
| $\# 6(12)$ | 12 |
| $\# 7(15)$ | 15 |
| $\# 8(8)$ | 8 |
| Total (100) | 100 |

Exam content is on both sides of the exam sheets.

Enter your answers in the boxes designated for each problem. Show your work for potential partial credit.

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## Problem 1. Give a Little Bit (15 points)

A. (2 points) Consider this code:

```
uint8_t a = 0x56;
uint8_t b = 0b10101010;
uint8_t c = 3;
```

Given the variable initializations above, evaluate (a \&\& b) | c. Provide your answer in both unsigned 8 -bit binary and decimal encodings.

| Unsigned 8-bit binary (0b): |
| :--- |
| 0000_0011 |
| Decimal: |
|  |

B. (2 points) Convert 16 to 8 -bit two's complement binary and hexadecimal encoding:

| 8 bit two's complement binary (0b): |
| :--- |
| $0001 \_0000$ |
| 8 bit two's complement hexadecimal ( 0 x ): |
| 10 |

C. (2 points) Convert -16 to 8 -bit two's complement binary and hexadecimal encoding:

| 8 bit two's complement binary (0b): |
| :--- |
| $1111 \_0000$ |
| 8 bit two's complement hexadecimal ( 0 x ): |
| F0 |

D. (2 points): An 8 -bit C variable contains the value $0 x E 0$. What would the decimal value be if the variable was a uint8_t? An int8_t?

| uint8_t decimal value: |  |
| :--- | :--- |
|  |  |
| int8_t decimal value: |  |
|  | -324 |

E. (2 points): Consider this code:

```
int8_t y = 0x7;
int8_t z = 0b10000001;
```

Evaluate the two operations and provide the resulting value in decimal form:

| $y \ll 2$ (in decimal): |  |
| :--- | :--- |
|  |  |
| $z \gg 1$ (in decimal): |  |
|  |  |
|  |  |
|  |  |

F. (2 Points) Consider this code:

```
int8_t x = 0xEF;
int8_t y = 0x1A;
int8_t z = x+y;
uint8_t a = 250;
uint8_t b = 7;
uint8_t c = a+b;
```

After this code executes, what are the decimal values of $z$ and $c$ ?

Value of $z$ (in decimal): 9

Value of c (in decimal): 1
G. (3 Points) What is the 32-bit floating point representation of the number -128.0? The format of 32-bit floating point encoding is shown below. Show your work for full credit. Note that the number shown in the figure is not-128.0.


$$
\text { Value }=(-1)^{\text {sign. }} \cdot 2^{\exp -127} \cdot\left(1+\sum_{i=1}^{23} b_{23-i} 2^{-i}\right)
$$

## 32 bit floating point representation of $\mathbf{- 1 2 8 . 0}$. Provide your answer in hexadecimal: <br> 0xC3000000

## Problem 2. Who Loves the Sum (6 points)

You are writing a function that computes the sum of the given array. Here is what you have so far.

```
// Computes the sum in the given array
// x: address of the first int in the array
// n: array length
int compute_sum(int* x, const unsigned int n) {
    int* y = x;
    int sum = 0;
    while (_BLANK 1__) {
        sum += __BLANK 2__;
        y += BLANK 3__;
    }
    return sum;
}
```

Fill in the blanks (using the table below) to complete the implementation.
Please note that you may not alter n because the variable is declared with the const (constant) keyword.

| BLANK 1: $y-x<n$ | BLANK 2: *y | BLANK 3: 1 |
| :---: | :---: | :---: |

## Problem 3: Hex's \& Oh's ( 10 points)

The $n$th hexagonal number can be calculated via the following formula:

$$
h_{n}=\frac{2 n \times(2 n-1)}{2}
$$

Please write an assembly procedure, hexagonal, that calculates the $n$th hexagonal number using the formula above. Its C declaration is: int hexagonal (int n) ; It should obey the RISC-V calling convention and return to its caller once it's done. Solutions that make unnecessary memory accesses will not be given full credit.

You have access to an additional instruction, mul, that performs integer multiplication. However, it is very slow so you may only use it once. The RISC-V ISA describes mul as:

| Inst. | Syntax | Description | Execution |
| :---: | :---: | :---: | :---: |
| MUL | mul rd, rs1, rs2 | Integer multiplication | $\operatorname{reg}[r d] \leftarrow(\operatorname{reg}[r s 1] * \operatorname{reg}[r s 2])[31: 0]$ |

In other words, it performs 32 bit * 32 bit multiplication and places the lower 32 bits of the product in rd. For this problem, we do not need to handle the case where the product is more than 32 bits. The encoding of mul is as follows:

| 25 | 24 | 2019 |  | 1514 | rs1 | funct3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| funct7 | rs2 | rd | opcode |  |  |  |
| 7 | 5 | 5 | 3 | 5 | 7 |  |

A. (8 points) Please write your implementation of hexagonal in the box below.

```
Hexagonal:
slli a0, a0, 1
addi a1, a0, -1
mul a0, a0, a1
srai a0, a0, 1
ret
OR
slli a1, a0, 1
addi a1, a1, -1
mul a0, a0, a1
ret
```

B. (2 points) How much space in memory (in bytes) does your implementation of hexagonal take up?

Number of bytes occupied by your hexagonal instructions: 4 * number of instructions

## Problem 4. Money, Money, Money (24 points)

A procedure is written in RISC-V assembly that calculates the composition of quarters ( 25 cents), dimes ( 10 cents), nickels ( 5 cents), and pennies ( 1 cent) needed to represent a certain amount of money specified in cents. The C definition is:
void makeChange(int amount, int* change_array);

- int amount: The amount of money (in US cents) to analyze
- int* change_array: An array used as the function's output. It lists the number of quarters, dimes, nickels, and pennies, at indices $0,1,2$, and 3 , respectively.

```
makeChange:
    addi sp, sp, -4
    sw ra, 0(sp)
quarter:
        addi t0, zero, 25
        bgt t0, a0, dime
        lw t1, 0(a1)
        addi t1, t1, 1
        sw t1, 0(a1)
        addi a0, a0, -25
        call makeChange
        j done
dime:
            addi t0, zero, 10
        bgt t0, a0, nickel
        lw t1, 4(a1)
        addi t1, t1, 1
        sw t1, 4(a1)
        addi a0, a0, -10
        call makeChange
        j done
nickel:
        addi t0, zero, 5
        bgt t0, a0, penny
        lw t1, 8(a1)
        addi t1, t1, 1
        sw t1, 8(a1)
        addi a0, a0, -5
        call makeChange
        j done
penny:
        addi t0, zero, 1
        bgt t0, a0, done
        lw t1, 12(a1)
        addi t1, t1, 1
        sw t1, 12(a1)
        addi a0, a0, -1
        call makeChange
        j done
done:
        lw ra, 0(sp)
        addi sp, sp, 4
        ret
```

The procedure is run. You are not given the value for amount, and change_array is an array that starts with zeroed-out elements. Eight coins are dispensed.

You obtain a stack trace from immediately after the procedure is run:


Answer the following questions:
A. (2 points) What is the value of the stack pointer ( sp ) at the time of the snapshot above?
$\square$
B. (2 points) What is the address of the instruction that makes the initial call to makeChange?
$\square$
C. (4 points) What are the final values in change_array after the call to makeChange?

$$
\{3,2,0,3\}
$$

D. (1 point) What is the value of input variable amount in the call to makeChange?
E. (5 points) What is the 32 bit value in memory address $0 \times 42000080$ ? Specify in binary or in hexadecimal.
$\square$
F. (10 points) Next, the following code is run (sp starts at $0 \times 3 f c 93 f 40)$ :

```
//int arrays coins_1 and coins_2 previously declared
for (int i=0; i<4; i++){
    coins_1[i] = 0;
    coins_2[i] = 0;
}
//time point 1
makeChange(52,coins_1); //corresponding call executed when pc=0x42004e18
//time point 2
makeChange(16,coins_2); //corresponding call executed when pc=0x42004e24
//time point 3
```

The values in a certain portion of memory are shown at time point 1. On the next page, fill in the values at time point 2 and time point 3.

Leave the cell blank if the values are unchanged from the values at time point 1.

| Address | time point 1 | time point 2 | time point 3 |
| :---: | :---: | :---: | :---: |
| $0 \times 3 f \mathrm{c} 93 \mathrm{f} 04$ | 0x00000001 |  |  |
| 0x3fc93f08 | 0x3fc91000 |  |  |
| 0x3fc93f0c | 0x00000000 |  |  |
| 0x3fc93f10 | 0x42004e2c |  |  |
| 0x3fc93f14 | 0x00000000 |  |  |
| 0x3fc93f18 | 0x00000000 |  |  |
| 0x3fc93f1c | 0x00000000 |  |  |
| 0x3fc93f20 | 0x00000000 |  |  |
| 0x3fc93f24 | 0x0000002a |  |  |
| 0x3fc93f28 | 0x00000111 |  |  |
| 0x3fc93f2c | 0xa0a0a0a0 | 0x420000a8 | $0 \times 420000 a 8$ |
| $0 \times 3 f c 93 f 30$ | 0x0000008a | 0x420000a8 | 0x420000a8 |
| 0x3fc93f34 | 0x0000008a | 0x42000048 | 0x42000088 |
| $0 \times 3 f c 93 f 38$ | 0x42004e6a | 0x42000048 | 0x42000068 |
| 0x3fc93f3c | 0x42004e6a | 0x42004e1c | 0x42004e28 |
| 0x3fc93f40 | 0x00000000 |  |  |
| 0x3fc93f44 | 0x00000001 |  |  |
| 0x3fc93f48 | 0x00000004 |  |  |
| 0x3fc93f4c | 0x00000003 |  |  |
| $0 \times 3 f c 93 f 50$ | 0x420165ac |  |  |
| 0x3fc93f54 | 0x420165b0 |  |  |
| 0x3fc93f58 | 0x12004e2c |  |  |
| 0x3fc93f5c | 0x00000000 |  |  |

## Problem 5: COPYCAT (12 points)

Belly Eyelash is writing an assembly program that she can use to retrieve information from different sources.

Part of this program is a procedure, arr_copy, that copies the values of an input array into an output array. It uses one other procedure, copy. Belly does not have access to the C or assembly implementations of copy, but she can assume that it works as expected and follows the RISC-V calling convention.

| arr_copy | copy |
| :---: | :---: |
| Arguments: | Arguments: |
| 1. int *src - pointer to input array | 1. int *src - pointer to input array |
| 2. int *dest - pointer to destination array | 2. int *dest - pointer to destination array |
| 3. int length - length of source array | 3. int idx - index of element to copy |
| Copies all length elements in the input array (src) into another array (dest). | Copies src[idx] into dest[idx] |
| Returns nothing | Returns nothing |

She uses a working C implementation of arr_copy for reference.

| Working C Implementation | Belly's Assembly Implementation |
| :---: | :---: |
| ```void arr_copy(int *src, int *dest, int length) { int i = 0; while (i < length) { copy(src, dest, i); i++; } }``` | ```arr_copy: li s0, 0 mv s1, a2 j compare loop: mv a2, s0 call copy addi s0, s0, 1 compare: blt s0, s1, loop ret``` |

The code compiles, however, it runs into some issues at run-time. Please answer the questions on the following page.

Please provide a short explanation for the following run-time behaviors. The entire assembly program works as expected when she uses the C implementation of arr_copy rather than her assembly version, so she has narrowed down the root cause to her assembly implementation of arr_copy.
A. (4 points) Belly's processor crashes due to an instruction accessing a memory address that it is not allowed to. This occurs at the instruction lwso, $0(a 0)$ within the copy procedure. She already used a debugger to verify that the correct arguments were passed into arr_copy.

Explanation: arr_copy does not save a0 before calling copy (or restore it after returning from copy). So, copy could have overwritten the value of a0 to be some value that, when used as a memory address, would result in an illegal memory access.
B. (4 points) Belly observes that her program gets trapped in an infinite loop within arr_copy. She already used a debugger to verify that the correct arguments were passed into arr_copy.

Explanation: arr_copy does not save ra before calling copy (or restore it after returning from copy). However, ra gets overwritten by the call copy instruction. Since the old value of ra (which would refer to an instruction outside of arr_copy; specifically the instruction after the one that called arr_copy) was not saved to the stack, there is no way to recover it and return to the proper instruction in the program. So, when arr_copy encounters the ret instruction, it will jump to the addi s0, s0, 1 instruction within arr_copy.
C. (4 points) Belly's processor crashes (again) due to an instruction accessing a memory address that it is not allowed to. This time, it occurs after arr_copy returns back to its caller procedure, at the instruction lw t1, 0 (s1). She already used a debugger to verify that arr_copy wrote to the destination array as expected.

> Explanation: arr_copy uses $s 0$, which is a callee-saved register, without saving its initial value to the stack and restoring it before returning. However, the procedure that called arr_copy was expecting $\mathbf{s} 0$ to be a particular value. Because arr_copy overwrites the value of $\mathbf{s} 0$ without restoring it to its initial value, the value in $\mathbf{s} 0$ may no longer be a valid memory address.

## Problem 6. Lights on Broadway (10 points)

As you remember from the labs and postlabs, our lab kit's display is an $8 \times 32$ array of LEDs that we control through a length-8 uint32_t array. You can assume the zeroth bit of the zeroth array element corresponds with the upper right corner of the display. We'd like to make a border-scrolling LED pattern where a single illuminated LED traces the entire border in a clockwise fashion, like shown below:


Your friend started implementing a function, chasingBorder, that takes in a pointer to the screen array, sb, and based on the array's state, updates it to the next appropriate value in the border animation. Complete the function so that each call to the function chasingBorder moves the illuminated LED one spot in the clockwise direction. You can assume the LEDs are already following this border-scrolling pattern when chasingBorder is called. You should not use any helper functions from lab.

Unfortunately, you spilled boba on your keyboard, disabling the ' [' and ']' keys, so you can't use them in your code. Fill in the ten blanks in the code below using the table on the next page.

```
void chasingBorder(uint32_t* sb){
    if(__BLANK 1_____){
        //move right
                    BLANK 2
```

$\qquad$

``` ;
        return;
    } else {
        //move down
        for(int i = 0; i < 7; i++){
            if (___BLANK 3_____){
                            BLANK 4___;
                            BLANK 5____
                return;
            }
        }
    }
    if (__________________
        //move left
                    BLANK 7
```

$\qquad$

```
        return;
    } else {
        //move up
        for(int i = 0; i < 7; i++){
            if (________){
            __BLANK 9__;
                        return;
            }
        }
    }
}
```

| Blank \#: | Line of Code: |
| :---: | :---: |
| BLANK 1 | *sb \& ! ${ }^{*}$ (sb == 1) OR *sb>1 |
| BLANK 2 | *sb >>= 1 or *sb $=* s b \gg 1$ |
| BLANK 3 | * $(\mathrm{sb}+\mathrm{i})==1$ |
| BLANK 4 | $*(s b+i)=0$ or 3 and 4 can be interchanged |
| BLANK 5 | * $(\mathrm{sb}+\mathrm{i}+1)=1$ |
| BLANK 6 | *(sb + 7) \&\& ! (* sb + 7) == (1 << 31) ) |
| BLANK 7 | *(sb + 7) <<= 1 |
| BLANK 8 | * $\mathrm{sb}+7-\mathrm{i})==(1 \ll 31)$ |
| BLANK 9 | $*(s b+7-i)=0$ or 8 and 9 can be interchanged |
| BLANK 10 | *(sb + $6-\mathrm{i})=(1 \ll 31)$ |

Could also do. (going down on left side instead of up)

| BLANK 8 | $*(\mathrm{sb}+\mathrm{i}+1)!=0$ |
| :--- | :--- |
| BLANK 9 | $*(\mathrm{sb}+\mathrm{i})=*(\mathrm{sb}+\mathrm{i}+1)$ |
| BLANK 10 | $*(\mathrm{sb}+\mathrm{i}+1)=0$ |

## Problem 7. MM..FOOD (15 Points)

We're in charge of managing a BurgerTime franchise which serves meals that look like this:

```
struct Meal{
    uint16_t burger;
    uint8_t fries;
};
```

We are going to focus on the burgers. Each burger contains only four possible ingredients: patties, cheese, tomatoes, and pickles. A burger is represented by a uint16_t that uses four bits to represent the count of each ingredient, so each burger can contain up to 15 units of each ingredient.

| Ingredient | Pickles |  |  |  | Tomatoes |  |  |  |  | Cheese Slices |  |  |  |  | Patties |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: |
| Burger bits | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |  |  |  |

A. (7 points) Due to popular demand, corporate has requested a function that can quickly remove pickles from a meal's burger. Write a function removePickles that takes in a pointer to a Meal struct, removes the pickles in the burger, and returns how many pickles were removed .

```
uint8_t removePickles(struct Meal *m){
    uint16_t burger = m->burger;
    uint16_t mask = 0xF << 12;
    m->burger &= ~mask;
    return (uint8_t)(burger >> 12);
```

\}
B. (8 points) Someone called in sick, and now it's on you to manage one of the stations.

Write a function called stationOne that adds patty_num patties, and tomato_num tomato slices to a meal's burger. You can assume the meal has no patties or tomato slices before the function is called.

```
void stationOne(struct Meal *m, uint8_t patty_num, uint8_t tomato_num){
    uint16_t mask = (patty_num & 0xF) | ((tomato_num & 0xF) << 8);
    m->burger |= mask;
```

\}

## Problem 8. The End (8 points)

Read through the following functions so that you understand what they do. An ASCII table is provided to you for reference in the exam Appendix. Assume that a char acts like an unsigned 8 bit integer.

```
#include <stdio.h>
void mystery1(char input) {
    for(int i=7; i>=0; i--) {
        printf("%d", (input >> i) & 1);
    }
    printf("\n");
}
char mystery2(char input) {
    input = ((0b11110000 & input) >> 4) | ((0b00001111 & input) << 4);
    input = ((0b11001100 & input) >> 2) | ((0b00110011 & input) << 2);
    input = ((0b10101010 & input) >> 1) | ((0b01010101 & input) << 1);
    return input & 0b11111111;
}
```

A. (4 points) Consider the test code below:
char input1 = 0b11001100;
mystery1(input1); // PRINT A
What will be printed by the line indicated by PRINT A?

| 11001100 |
| :--- |

B. (4 points) Consider the test code below:
char input2 = 'G';
mystery1(mystery2(input2)); // PRINT B
What will be printed by the line indicated by PRINT B?

This page intentionally left blank

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## Appendix 1: String functions

char *strcat (char *dest, const char *src) - appends the string pointed to by src to the end of the string pointed to by dest. This function returns a pointer to the resulting string dest.
char *strncat (char *dest, const char *src, size_t n) - appends the string pointed to by src to the end of the string pointed to by dest up to n characters long. This function returns a pointer to the resulting string dest.
char *strcpy (char *dest, const char *src) - copies the string pointed to, by src to dest. This returns a pointer to the destination string dest.
char *strncpy (char *dest, const char *src, size_t n) - copies up to n characters from the string pointed to, by src to dest. In a case where the length of src is less than that of $n$, the remainder of dest will be padded with null bytes. This function returns the pointer to the copied string.
int strcmp(const char *str1, const char *str2)- compares the string pointed to, by str1 to the string pointed to by str2. This function return values that are as follows -

- if Return value $<0$ then it indicates str1 is less than str2.
- if Return value $>0$ then it indicates str2 is less than str1.
- if Return value $=0$ then it indicates str1 is equal to str2.
int strncmp(const char *str1, const char *str2, size_t $n$ )-compares at most the first $n$ bytes of str1 and str2. This function return values that are as follows -
- if Return value $<0$ then it indicates str1 is less than str2.
- if Return value $>0$ then it indicates str2 is less than str1.
- if Return value $=0$ then it indicates str1 is equal to str2.
char ${ }^{*}$ strchr (const char *str, int c) - searches for the first occurrence of the character c (an unsigned char) in the string pointed to by the argument str. This returns a pointer to the first occurrence of the character $c$ in the string str, or NULL if the character is not found.
char *strrchr (const char *str, int c) - searches for the last occurrence of the character c (an unsigned char) in the string pointed to, by the argument str. This function returns a pointer to the last occurrence of character in str. If the value is not found, the function returns a null pointer.
char *strstr(const char *haystack, const char *needle)-function finds the first occurrence of the substring needle in the string haystack. The terminating ' $\backslash 0$ ' characters are not compared. This function returns a pointer to the first occurrence in haystack of any of the entire sequence of characters specified in needle, or a null pointer if the sequence is not present in haystack.
char *strtok(char *str, const char *delim)-breaks string str into a series of tokens using the delimiter delim. This function returns a pointer to the first token found in the string. A null pointer is returned if there are no tokens left to retrieve.


## Appendix 2: ASCII Table

ASCII Table

| Dec | Hex | Oct Char | Dec | Hex | Oct | Char | Dec | Hex | Oct | Char | Dec | Hex | Oct | Char |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 32 | 20 | 40 | [space] | 64 | 40 | 100 | @ | 96 | 60 | 140 | - |
| 1 | 1 | 1 | 33 | 21 | 41 | ! | 65 | 41 | 101 | A | 97 | 61 | 141 | a |
| 2 | 2 | 2 | 34 | 22 | 42 | " | 66 | 42 | 102 | B | 98 | 62 | 142 | b |
| 3 | 3 | 3 | 35 | 23 | 43 | \# | 67 | 43 | 103 | C | 99 | 63 | 143 | c |
| 4 | 4 | 4 | 36 | 24 | 44 | \$ | 68 | 44 | 104 | D | 100 | 64 | 144 | d |
| 5 | 5 | 5 | 37 | 25 | 45 | \% | 69 | 45 | 105 | E | 101 | 65 | 145 | e |
| 6 | 6 | 6 | 38 | 26 | 46 | \& | 70 | 46 | 106 | F | 102 | 66 | 146 | $f$ |
| 7 | 7 | 7 | 39 | 27 | 47 | , | 71 | 47 | 107 | G | 103 | 67 | 147 | g |
| 8 | 8 | 10 | 40 | 28 | 50 | ( | 72 | 48 | 110 | H | 104 | 68 | 150 | h |
| 9 | 9 | 11 | 41 | 29 | 51 | ) | 73 | 49 | 111 | I | 105 | 69 | 151 | i |
| 10 | A | 12 | 42 | 2A | 52 | * | 74 | 4A | 112 | J | 106 | 6 A | 152 | j |
| 11 | B | 13 | 43 | 2B | 53 | + | 75 | 4B | 113 | K | 107 | 6B | 153 | k |
| 12 | C | 14 | 44 | 2C | 54 | , | 76 | 4C | 114 | L | 108 | 6C | 154 | 1 |
| 13 | D | 15 | 45 | 2D | 55 | - | 77 | 4D | 115 | M | 109 | 6D | 155 | m |
| 14 | E | 16 | 46 | 2E | 56 | . | 78 | 4E | 116 | N | 110 | 6E | 156 | n |
| 15 | F | 17 | 47 | 2F | 57 | 1 | 79 | 4F | 117 | O | 111 | 6 F | 157 | 0 |
| 16 | 10 | 20 | 48 | 30 | 60 | 0 | 80 | 50 | 120 | P | 112 | 70 | 160 | p |
| 17 | 11 | 21 | 49 | 31 | 61 | 1 | 81 | 51 | 121 | Q | 113 | 71 | 161 | q |
| 18 | 12 | 22 | 50 | 32 | 62 | 2 | 82 | 52 | 122 | R | 114 | 72 | 162 | r |
| 19 | 13 | 23 | 51 | 33 | 63 | 3 | 83 | 53 | 123 | S | 115 | 73 | 163 | S |
| 20 | 14 | 24 | 52 | 34 | 64 | 4 | 84 | 54 | 124 | T | 116 | 74 | 164 | t |
| 21 | 15 | 25 | 53 | 35 | 65 | 5 | 85 | 55 | 125 | U | 117 | 75 | 165 | u |
| 22 | 16 | 26 | 54 | 36 | 66 | 6 | 86 | 56 | 126 | V | 118 | 76 | 166 | v |
| 23 | 17 | 27 | 55 | 37 | 67 | 7 | 87 | 57 | 127 | W | 119 | 77 | 167 | w |
| 24 | 18 | 30 | 56 | 38 | 70 | 8 | 88 | 58 | 130 | $X$ | 120 | 78 | 170 | x |
| 25 | 19 | 31 | 57 | 39 | 71 | 9 | 89 | 59 | 131 | Y | 121 | 79 | 171 | $y$ |
| 26 | 1A | 32 | 58 | 3 A | 72 | : | 90 | 5A | 132 | Z | 122 | 7 A | 172 | z |
| 27 | 1B | 33 | 59 | 3B | 73 | ; | 91 | 5B | 133 | [ | 123 | 7B | 173 | \{ |
| 28 | 1 C | 34 | 60 | 3C | 74 | $<$ | 92 | 5C | 134 | 1 | 124 | 7 C | 174 | \| |
| 29 | 1D | 35 | 61 | 3D | 75 | $=$ | 93 | 5D | 135 | ] | 125 | 7D | 175 | \} |
| 30 | 1E | 36 | 62 | 3E | 76 | > | 94 | 5E | 136 | ヘ | 126 | 7E | 176 | $\sim$ |
| 31 | 1 F | 37 | 63 | 3F | 77 | ? | 95 | 5F | 137 | - | 127 | 7F | 177 |  |

## Appendix 3: C Operator Precedence

| Precedence | Operator | Description | Associativity |
| :---: | :---: | :---: | :---: |
| 1 | ++ -- | Suffix/postfix increment and decrement | Left-to-right |
|  | () | Function call |  |
|  | [] | Array subscripting |  |
|  | - | Structure and union member access |  |
|  | -> | Structure and union member access through pointer |  |
| 2 | ++ -- | Prefix increment and decrement | Right-to-left |
|  | + | Unary plus and minus |  |
|  | ! ~ | Logical NOT and bitwise NOT |  |
|  | (type) | Cast |  |
|  | * | Indirection (dereference) |  |
|  | \& | Address-of |  |
| 3 | * / \% | Multiplication, division, and remainder | Left-to-right |
| 4 | + - | Addition and subtraction |  |
| 5 | << >> | Bitwise left shift and right shift |  |
| 6 | \ll= | For relational operators $<$ and $\leq$ respectively |  |
|  | \gg= | For relational operators $>$ and $\geq$ respectively |  |
| 7 | == ! $=$ | For relational $=$ and $\neq$ respectively |  |
| 8 | \& | Bitwise AND |  |
| 9 | $\wedge$ | Bitwise XOR (exclusive or) |  |
| 10 | \| | Bitwise OR (inclusive or) |  |
| 11 | \&\& | Logical AND |  |
| 12 | \| $\mid$ | Logical OR |  |
| 13 | ? : | Ternary conditional | Right-to-left |
| 14 | = | Simple assignment |  |
|  | += | Assignment by sum and difference |  |
|  | *= /= \%= | Assignment by product, quotient, and remainder |  |
|  | <<= >>> | Assignment by bitwise left shift and right shift |  |
|  | \& ${ }^{\wedge}=1=$ | Assignment by bitwise AND, XOR, and OR |  |

